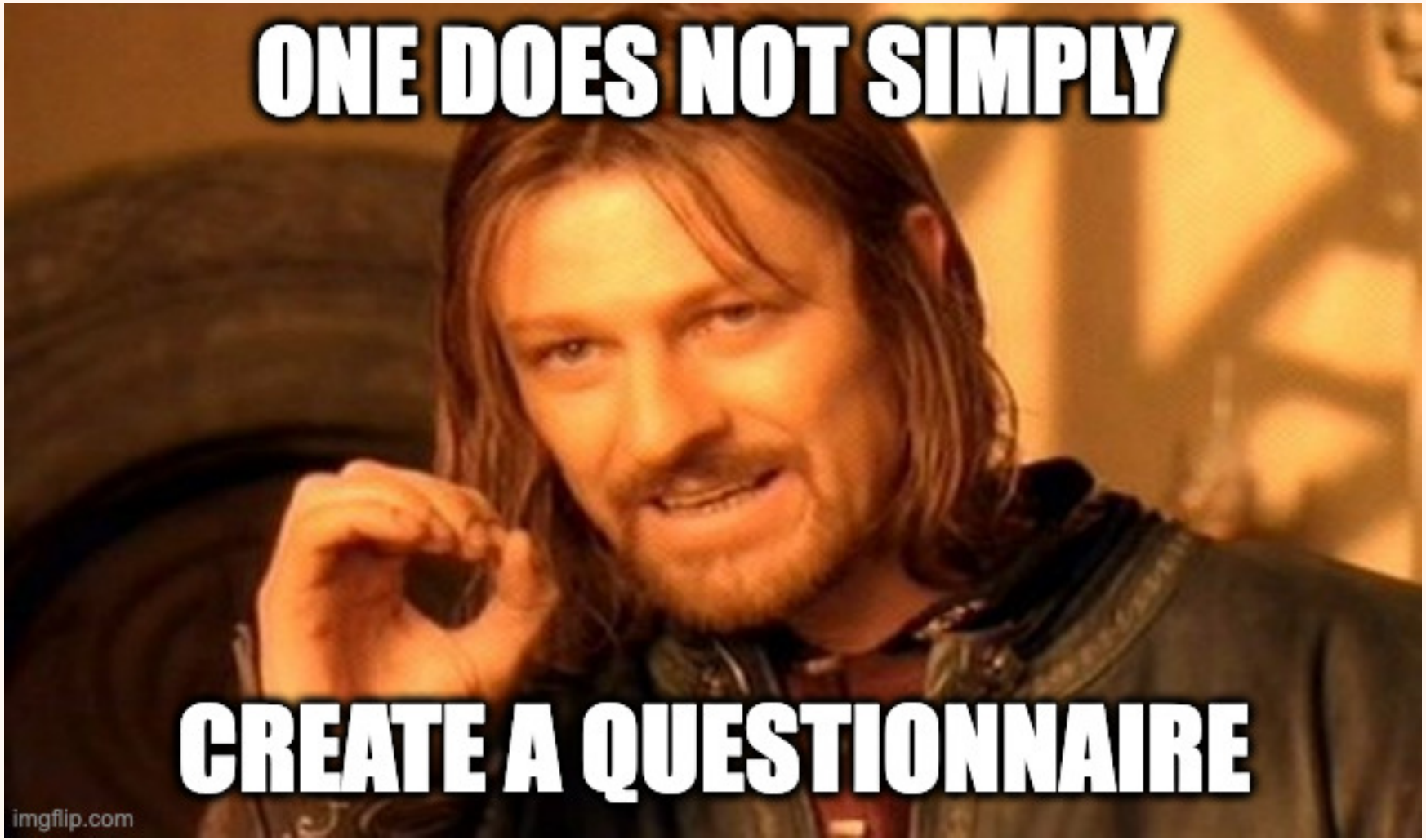
Dependent types are everywhere!

With application to questionnaires


ONE DOES NOT SIMPLY
CREATE A QUESTIONNAIRE
imgflip.com

Dependent types

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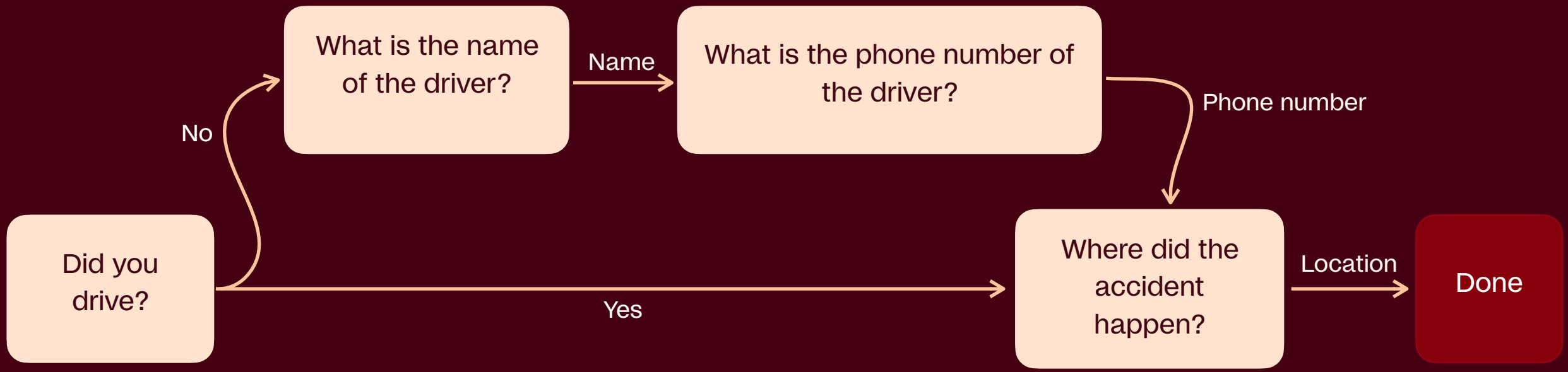
safeGet : (list : List a) -> (i : Index list) -> a
safeGet = ...
```


OOP
FP
FP WITH DEPENDENT TYPES
imgflip.com

Questionnaires are dependently typed!



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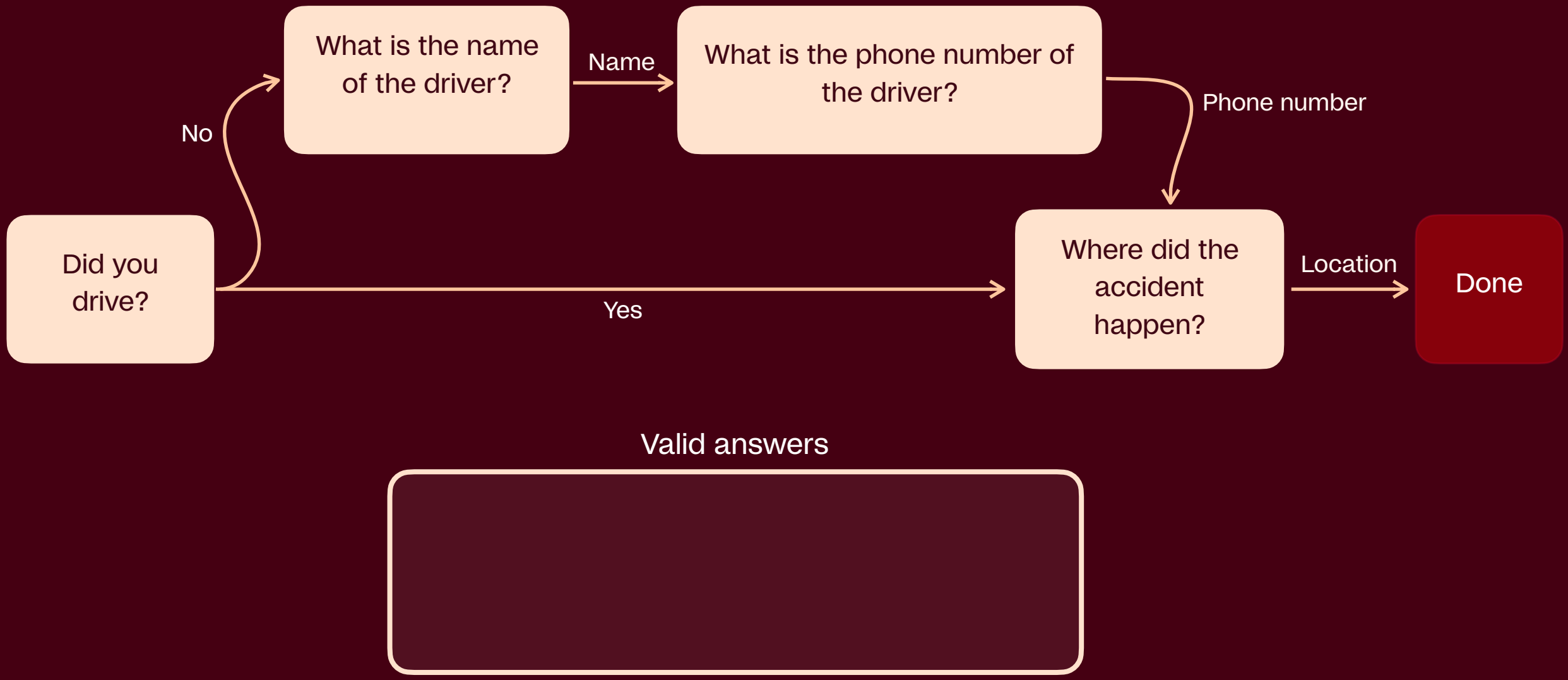

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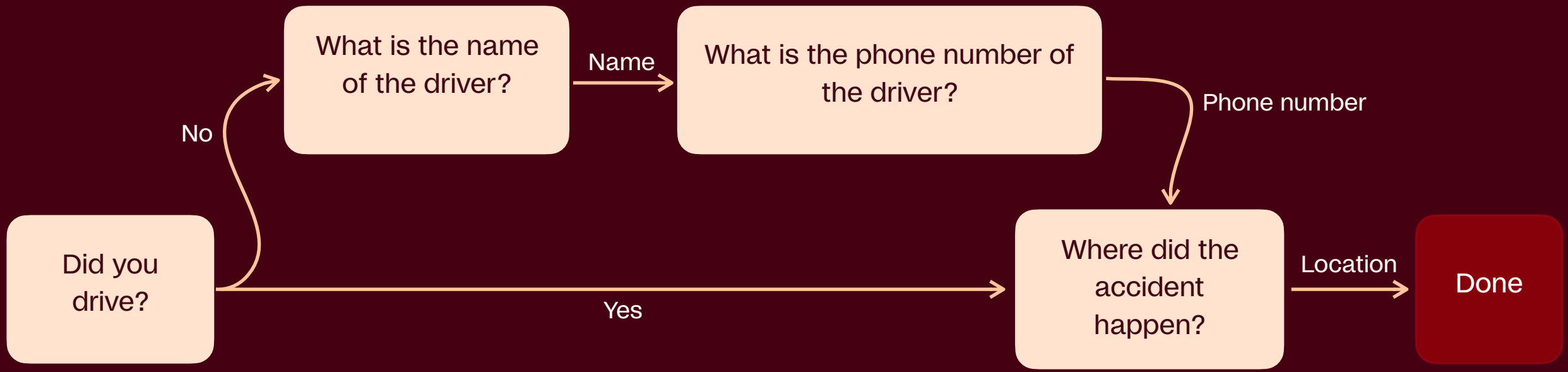

Valid answers

Yes → Within Norway

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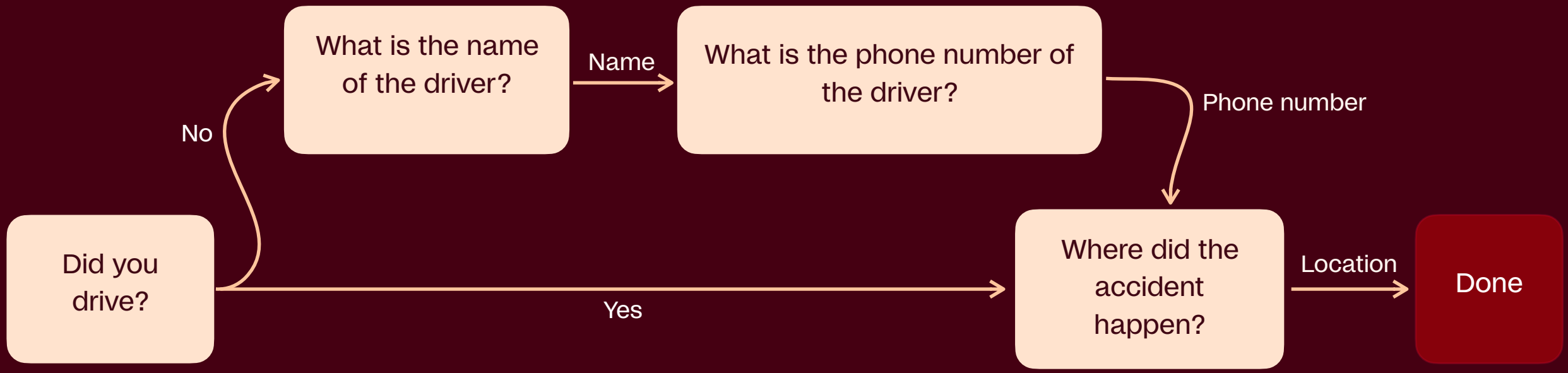

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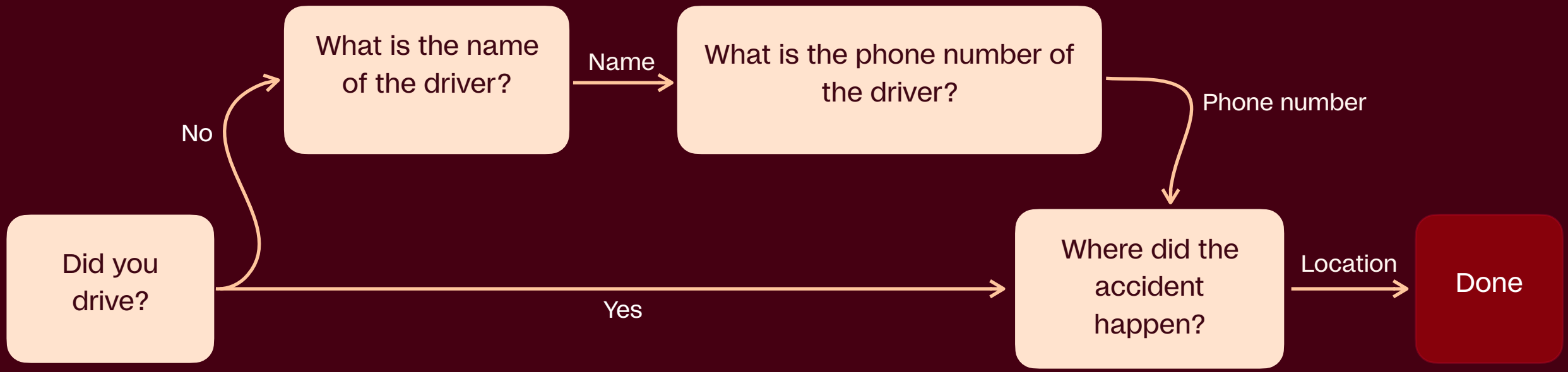

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Yes → Within Norway
No → "Hatti Fnatt" → 947 82 456 → Outside Norway
No → "Pelle Pang" → 473 62 115 → Within Norway

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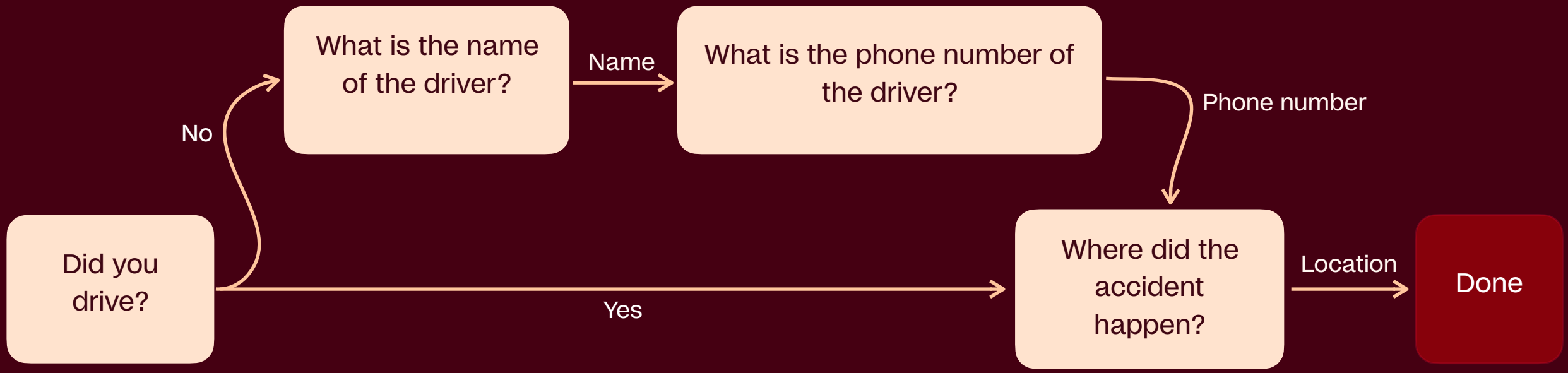

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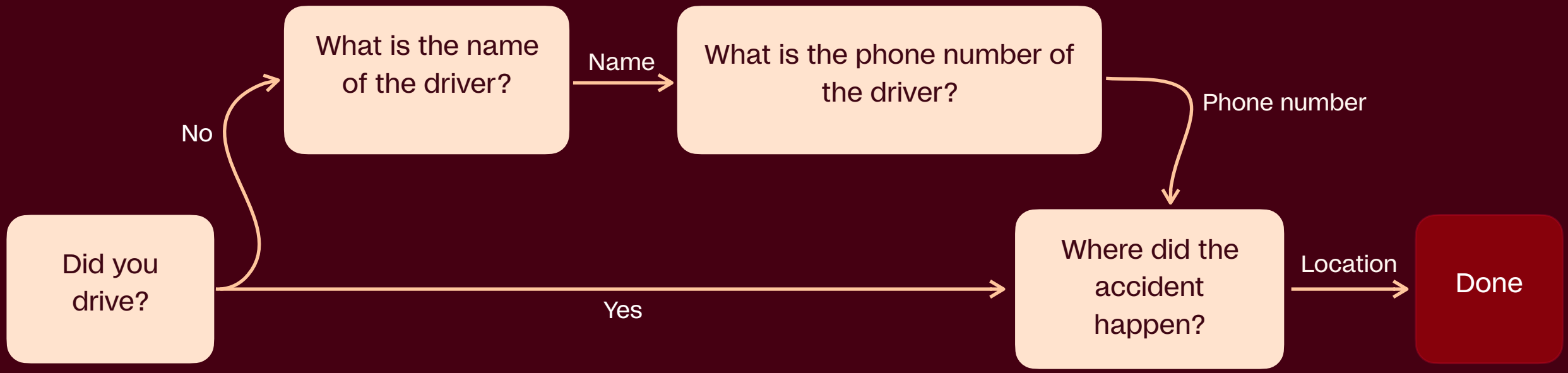

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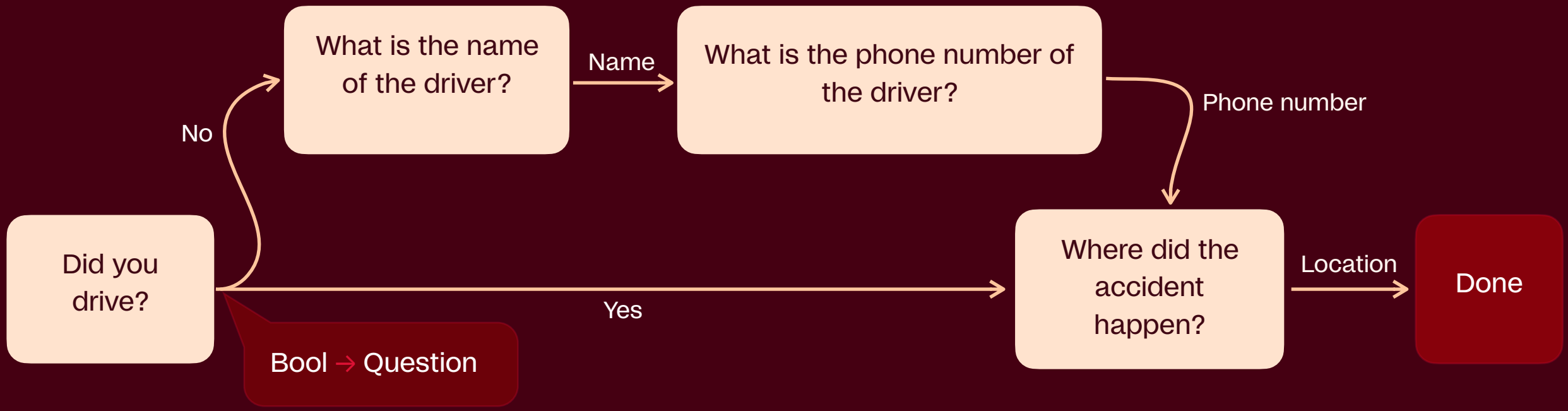

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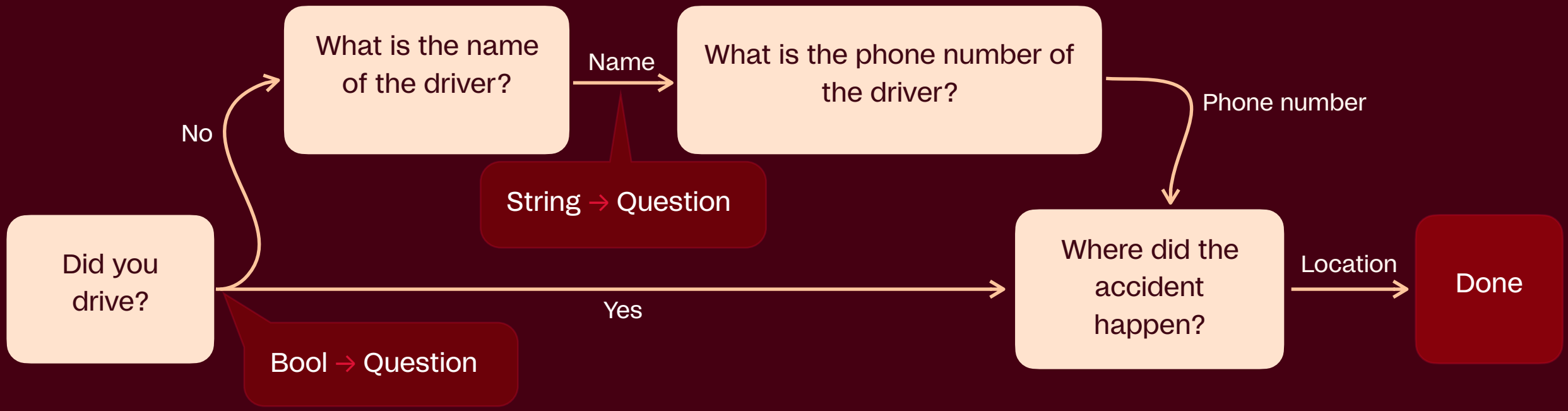

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Demo

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